

## Sign In

- Website: <https://goo.gl/forms/FzHS5sINK1aW1LJC3>
- Enter the word of the day in the appropriate slot.

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## Lecture #4: Simple Compression: Huffman Trees

- Strings are composed of characters, which (like everything else in a computer) are represented as bit strings.
- The relationship between characters and their bit representations (*encodings* or *code points*) is arbitrary. Standardization is necessary to prevent chaos.
- Python now uses an international standard known as *Unicode*, which encodes (as of Version 9.0) 128,237 characters, using code points that range from 0–1,114,111.
- These cover 135 scripts (roughly, alphabets), and various sets of symbols: punctuation, control characters (like tab or newline), mathematical symbols, etc.
- A few examples:

Literal	Glyph	Encoding	Glyph	Encoding	Glyph
<code>"\u0041"</code>	A	<code>"\u0041"</code>	À	<code>"\u00398"</code>	☹
<code>"\u0061"</code>	a	<code>"\u0061"</code>	á	<code>"\u2663"</code>	♣
<code>"\u0030"</code>	0	<code>"\u00E9"</code>	é	<code>"\u2639"</code>	☹
<code>"\u0040"</code>	@	<code>"\u05D0"</code>	ℵ		

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## More Efficient Encoding

- If every character in a text is represented by an integer value in the full range, we'd have 3 bytes (24 bits) per character.
  - So usually, the code points themselves are encoded.
  - One common encoding, *UTF-8*, uses 1–4 bytes per character, depending on the number of significant bits in the code point.
- | Bits Coded | Range of code points | Byte 1   | Byte 2   | Byte 3   | Byte 4   |
|------------|----------------------|----------|----------|----------|----------|
| 7          | 0x0000 .. 0x007F     | 0xxxxxxx |          |          |          |
| 11         | 0x0080 .. 0x07FF     | 110xxxxx | 10xxxxxx |          |          |
| 16         | 0x0800 .. 0xFFFF     | 1110xxxx | 10xxxxxx | 10xxxxxx |          |
| 21         | 0x10000 .. 0x10FFFF  | 11110xxx | 10xxxxxx | 10xxxxxx | 10xxxxxx |
- X's mark places containing the bits of the code points. The other bits flag how many bytes are needed.
  - Where one-byte characters are common, this saves space.
  - One clever feature is that bytes 2–4 (continuation bytes) all start with a distinctive pattern (10), so that if one starts at any byte in an array of bytes, one can find the beginning of the character.

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## Unique Prefix Property

- This ambiguity problem can be solved by choosing a code with the *Unique Prefix Property*: The bit encoding for any character is never a prefix of the encoding of any other character.
- For example, the encoding  
E => 0, T => 10, A => 1101, O => 1100, I => 1110, ...
- has this property (at least for the characters shown). No encodings appears at the beginning of any other.
- Eg., "TEE" encodes to 1000, "AE" to 11010, and "I" to 1110.
- There is never any ambiguity about where a character begins, if one works from the left.
- Starting from a given bit position, *n*, as soon as one collects bits that match the encoding of character *C*, we know that *C* has to be the character that starts at *n*, since adding more bits can never match another character.

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## Still More Efficient

- We can, however, do better still by using other variable-length encodings that can use less than a byte per character.
- There's potential problem with this idea, however: ambiguity.
- Suppose we tried an encoding like this, using shorter codes for more common letters:  
E => 0, T => 1, A => 10, O => 11, I => 100, ...
- And suppose we receive the bits 100.
- Is this "TEE", "AE", or "I"? Where does one letter end and the next begin?

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## Decoding Using the Unique Prefix Property

- Given a bit encoding with the unique prefix property, how do we decode?
- Discussion in previous slide gives one solution using a dictionary to map encodings to characters.
- For simplicity, imagine our encoded text as a string of 0s and 1s (not a representation you'd actually use in practice).
- Suppose *D* is a dictionary from such strings of 0s and 1s to characters. Then,

```
def decode(msg):
    """Convert encoded message MSG into the character string it represents."""
    ch = ""
    result = ""
    for b in msg:
        ch += b
        if ch in D:
            result += D[ch]
            ch = ""
```

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